

GAUGE: the GrAnd Unification and Gravity Explorer

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Abstract The GAUGE (GrAnd Unification and Gravity Explorer) mission proposes to use a drag-free spacecraft platform onto which a number of experiments are attached. They are designed to address a number of key issues at the interface between gravity and unification with the other forces of

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nature. The equivalence principle is to be probed with both a high-precision test using classical macroscopic test bodies, and, to lower precision, using microscopic test bodies via cold-atom interferometry. These two equivalence principle tests will explore string-dilaton theories and the effect of space–time fluctuations respectively. The macroscopic test bodies will also be used for intermediate-range inverse-square law and an axion-like spin-coupling search. The microscopic test bodies offer the prospect of extending the range of tests to also include short-range inverse-square law and spin-coupling measurements as well as looking for evidence of quantum decoherence due to space–time fluctuations at the Planck scale.

Keywords Fundamental physics · Space mission · Equivalence principle · Mass–spin coupling · Atom interferometry

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1 Introduction

GAUGE (GrAnd Unification and Gravity Explorer) is a proposal to the Cosmic Visions programme at ESA. The proposal is for a drag-free spacecraft platform onto which is attached a number of modular experiments. A complement of experiments is designed to address a number of key issues at the interface between gravity and unification with the other forces of nature. We include:

- A test of string-dilaton theories using a high precision macroscopic equivalence principle experiment, MEPE
- A test of the effect of quantum space–time fluctuations in a microscopic equivalence principle experiment, QSTEP
- A $1/r^2$ test at intermediate ranges, IRISL
- An intermediate range axion-like mass–spin coupling search, IRSC
- Measurement of quantum decoherence from space–time fluctuations at the Planck scale, QDE

In addition there are some exciting options which need more study to confirm their feasibility and sensitivity. These are short range tests of the inverse square law (SRISL) and spin-coupling forces (SRSC) at distances of a few microns, which would provide a test of extra dimensions. MEPE will achieve an equivalence principle test between classical macroscopic test masses to 1 part in 10^{18} . The experiment concept is simply to put test mass pairs into free-fall around the Earth in what is essentially a repeat of Galileo's experiment. Four test mass pairs with three different materials are used to provide a

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cyclic closure condition and a null test. The technology is sound and mature. QSTEP is also an equivalence principle test but this time using atomic species, Rb and Cs and will achieve 1 part in 10^{15} . Even though it is less sensitive than MEPE it will allow a meaningful test within a quantum space–time fluctuation which MEPE could not. ISL will allow searches for inverse square law deviations at two scale lengths; intermediate using classical proof mass technology and short-range using atom interferometry. SC will allow searches for spin-mass coupling at two scale lengths; intermediate using classical proof mass technology and short-range using atom interferometry. QDE will use atom interferometry to look for fundamental limitations to the quality of matter wave interference patterns due to space–time fluctuations. MEPE and some parts of IRISL and IRSC rely on superconducting technology and hence require low temperature operation inside a liquid helium dewar. QSTEP, SRISL, SRSC and QDE require the use of atom interferometry and this is a room temperature technology. The cold experiments will be accommodated inside a liquid helium dewar which is attached to the spacecraft. The warm experiments will fit inside the spacecraft bus itself. The payload can be accommodated on a replica of the LISA Pathfinder bus. The bus should also include the LTP sensors to provide drag-free capability at the bus level as well as take part in some of the experiments themselves. The whole spacecraft is then compatible with a launch on VEGA into a sun-synchronous orbit. The experiments will be carried out in sequence starting with those dependent on the helium supply. The overall mission duration will be 2 years.

2 Scientific objectives

GAUGE proposes new tests of general relativity (GR) in Earth-orbit that will include the Einstein equivalence principle (EEP), the inverse square law, spin-coupling and the quantum vacuum. This will be done using a combination of macroscopic test masses and matter wave interferometry in a drag-free spacecraft.

2.1 The equivalence principle

The EEP is the basis of Einstein’s theory of GR and is one of the most enduring invariants of nature. There are good reasons based on current theoretical models looking for a unified quantum theory of matter and fields that this invariance will break down at levels below the present limits. In these models GR, though very nearly true, describes a field structure that evolved from a more complex unified field structure in the early universe that violated the equivalence principle. GAUGE will therefore have a direct bearing on the “Structure and Evolution of the Universe”, as well as probing the standard model (SM) of particle physics. The SM predicts a grand unification of the forces of nature at the grand unification theory (GUT) scale. There is experimental evidence for unification of the electromagnetic and weak forces, but the

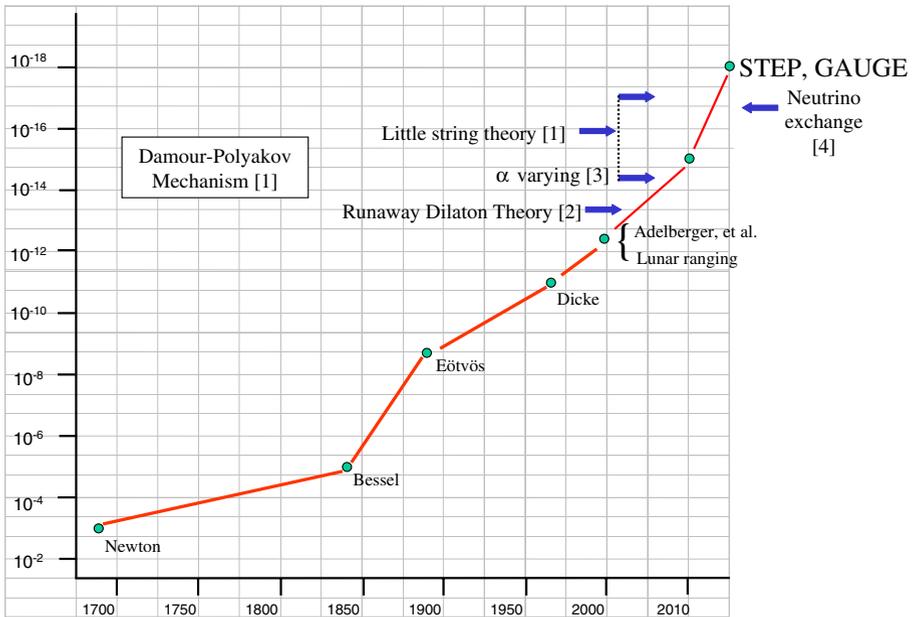


Fig. 1 Progression in sensitivity of EP measurements

resulting electro-weak force still remains distinct from the strong force but with a trend to unify at the GUT scale. These forces remain totally disconnected from the force of gravity. Another problem arising with the standard model is the “gauge hierarchy problem”. Electroweak unification occurs through a matching of forces at one mass scale, but the mass scale for grand unification differs from this by a factor 10^{12} well beyond test using present and future particle accelerators. The pursuit of unification through string theory and supersymmetry has resulted in the need to involve extra dimensions and naturally energizing new long range forces with strength comparable to or weaker than gravity. These forces couple not to mass, but to other properties of the atom like baryon and lepton number in various combinations, and they may violate the equivalence principle at a level that is measurable by GAUGE (see [1, 2] and Fig. 1). Also shown is the predicted level at which cosmological models incorporating a time varying alpha invoke violations [3] and the level at which an anomalous coupling to the weak interaction could appear due to neutrino-antineutrino exchange [4]. An EEP violation would confirm the existence of new forces. A confirmation to one part in 10^{18} would extend GR theory and restrict the existence of new ultra-weak long-range forces causing a major problem for “string theory”.

2.2 Inverse square law

The inverse square law can be checked with both classical and quantum detectors on GAUGE. GAUGE will use pairs of masses to measure force

changes as one of the masses is moved. The inverse square law is well-tested for planetary astrophysical distances but not for distances of microns or less. Models that go beyond the SM such as string theory and supersymmetry aiming at unification have, as a natural consequence, new long range forces with strengths comparable or weaker than gravity. GAUGE will be able to look for violations of Newton's law confirming new long range forces on both intermediate (~ 20 cm) and possible short range (~ 10 μm).

2.3 Spin coupling

In addition to new long range forces modern unification theories also predict the existence of new light-mass pseudoscalars. These give rise to a force between intrinsic quantum mechanical spin and mass. So far all attempts to detect spin-coupling forces either cosmologically or in the laboratory have produced only upper limits. Hypotheses about spin-mass coupling forces originate in attempts to resolve the problems of the standard model such as the charge parity conservation puzzle and the composition of dark matter. The existence of spin-mass coupling also implies a violation of the EEP. The SM is unquestionably a highly successful description of the electromagnetic, weak and strong interactions comprising the gauge symmetry groups $U(1) \times SU(2) \times SU(3)$. Although there is no current disagreement between experiment and theory the SM is known to have some shortcomings. Perhaps one of the most puzzling is the fact that the QCD Lagrangian contains a term that can violate CP symmetry

$$L = \theta \frac{\alpha}{8\pi} G^{\mu\nu} G_{\mu\nu} \quad (1)$$

where θ is an arbitrary parameter and $G^{\mu\nu}/G_{\mu\nu}$ are the gluon field tensors. Experimental limits on the electric dipole moment of the neutron suggest that this term is suppressed by 10 orders of magnitude ($\theta < 2.5 \times 10^{-10}$) and this is the well-known *strong CP problem*. An elegant solution to this problem is the addition of a additional $U(1)$ symmetry called the Peccei–Quinn group [5]. This symmetry is broken at an energy scale f_a and gives rise a spin-zero boson named the axion, whose field, Φ_a , couples to the gluon field via an additional term in the QCD Lagrangian

$$L = \left(\theta - \frac{\Phi_a}{f_a} \right) \frac{\alpha}{8\pi} G^{\mu\nu} G_{\mu\nu} \quad (2)$$

The axion potential is minimised when $\Phi_a = \theta \times f_a$ and the CP violating term is driven to zero. Although the axion is the best motivated spin-zero boson, in principle many axion-like particles could exist in nature. In general field theories that spontaneously break global symmetry result in a massless spin-zero Goldstone boson. If the symmetry is not exact the boson can acquire a small mass (as in the case of the axion). Other examples are the U-boson [6], the arion [7], the familon [8] and the dilaton [9]. Such particles have small masses and couple very weakly to normal matter, making them potential non-baryonic dark matter candidates.

Axions, and axion-like particles, couple to both the scalar (or spin independent) and pseudoscalar (spin dependant) vertex [10]. This causes three distinct interactions: scalar-scalar (mass–mass), scalar-pseudoscalar (mass–spin) and pseudoscalar-pseudoscalar (spin-spin). An interaction of the mass–mass type would lead to a violation of the inverse square law of gravity in the range $20\ \mu\text{m} < \lambda < 2\ \text{cm}$. However this is difficult to demonstrate in a “clean measurement” for axions. The spin-spin interaction is also difficult because the direct magnetic coupling between the aligned fermions (or spins) has to be shielded. As a result the most commonly measured interaction is the mass–spin. The interaction potential between a polarised spin σ and a nucleon is

$$V = g_p g_s \frac{\hbar^2}{8\pi m_e} \hat{\sigma} \cdot \hat{r} \left(\frac{1}{\lambda r} + \frac{1}{r^2} \right) \exp(-r/\lambda) \quad (3)$$

where $g_p g_s$ is a dimensionless coupling constant, m_e is the mass of the electron (assuming the aligned spins are polarised electrons) and λ is the interaction range. This interaction violates parity and time reversal symmetries. Its detection would be a first in nature. The axion is described by two parameters, f_a and θ to which the mass, range and coupling constants are related by:

$$m_a \simeq 10^{-5} \text{ eV} (10^{12} \text{ GeV}/f_a) \quad (4)$$

$$\lambda \simeq 2 \text{ cm} (f_a/10^{12} \text{ GeV}) \quad (5)$$

$$g_p g_s = \frac{\theta}{\lambda^2} \times 6 \times 10^{-33} \quad (6)$$

Astrophysical arguments constrain the mass and energy of the axion. Axions produced in stars and supernovae can escape easily and provide a significant cooling mechanism. The neutrino burst duration from SN1987A implied $m_a \leq 10\ \text{meV}$ and $\lambda \geq 20\ \mu\text{m}$ [11]. Conversely $m_a \geq 1\ \mu\text{eV}$ and $\lambda \leq 20\ \text{cm}$ come from a cosmological need to avoid their over-production in the early universe. Experimental searches probe axions either through their coupling to photons (2 photon–axion vertex) or through the mass–spin interaction of (3). The former are typically resonant cavity searches such as ADMX [12], the Cern-Axion-Solar-Telescope (CAST) [13] or the PVLAS [14] search for vacuum birefringence. The latter search for axions through their mass–spin (or spin-spin) interactions. At ranges $> 1\ \text{m}$, a torsion balance with an attached spin-polarised test-mass [15] sets the tightest constraints. In the range $10\ \text{cm} < \lambda < 1\ \text{m}$ the best constraints come from comparison of the relative precession frequencies of Hg and Cs magnetometers [16]. Several other experiments have placed limits at considerably shorter ranges. A DC SQUID magnetometer used to measure the change in polarisation of a paramagnetic salt induced by the motion of an unpolarised source mass [17] sets the strongest constraints for $5\ \text{mm} < \lambda < 10\ \text{cm}$. The best limits at ranges $< 5\ \text{mm}$ come from a spherical torsion balance operating at 4.2 K [18]. In this experiment unpolarised test masses located on the torsion balance are subjected to the possible axion field produced by a polarisable source of spins of the type proposed for GAUGE. The dimensionless coupling constant at a range of 1mm was reported to be $g_p g_s < 1.0 \times 10^{-24}$.

2.4 Quantum vacuum

2.4.1 Violation of equivalence principle at the atomic level

A number of models describe space–time fluctuations as small fluctuations of the metric on a given background metric. Even though the unification of quantum mechanics and gravitation is one of the big outstanding problems of contemporary physics there is no theory of quantum gravity. However, approaches like string theory or loop quantum gravity make some general predictions which may serve as guidance for experimental search. The difficulty is that in many cases the precise strength of the various expected effects are not known. Quantum gravity phenomenology tries to overcome this problem by parameterizing possible effects and working out experimental consequences for classes of phenomena. Different quantum gravity theories are characterized by different parameters. One class of expected effects of ‘quantum gravity’ is a non-trivial quantum-gravity vacuum (“space–time foam”) which can be regarded as a fluctuating space–time. Space–time fluctuations could lead to a minimal observable distance setting an absolute bound on the measurability of distances and defining a fundamental length scale [19, 20]. For instance the search for additional noise sources in gravitational wave interferometers was previously considered, and analyzed in the context of an experiments with optical cavities and resonators [21, 22]. A space–time foam may also violate the principle of equivalence as suggested by Ellis and coworkers [23]. Another prediction of quantum gravity models are so called deformed dispersion relations [24–27]. Hu and Verdauger [28] analyzed classical stochastic fluctuations of space–time geometry stemming from quantum fluctuations of matter fields in the context of semiclassical theory of gravity. This leads to a stochastic behaviour of the metric tensor. Effects of fluctuations of space–time geometry leading to, e.g., lightcone fluctuations, redshift and angular blurring were discussed in [30]. The analysis in [16] takes into account non-conformal fluctuations of the metric and yields a modified inertial mass subject to the stochastic properties. The dominant modification is through an anomalous inertial mass tensor which depends on particle type and fluctuation scenario. This necessarily violates the weak equivalence principle (WEP) and, in general, also Lorentz invariance. By means of the rescaled inertial mass and the dependency on particle type (Δt_p) one can guess that the WEP may be violated with a ratio of inertial to gravitational mass given by

$$\left(\frac{m_g}{m_i}\right)_p = 1 + \alpha(\gamma, \Delta t_p) \text{ with } \alpha(\gamma, \Delta t_p) = \Sigma_{j=1}^3 \langle \tilde{h}^{ij} \rangle \quad (7)$$

where the index p stands for “particle”. α is proportional to the particle resolution time Δt_p^{-1} and therefore, identifying the resolution scale with the Compton time, t_C , is subject to an amplification when large coherent states are chosen scaling with the number of particles. The resolution time for Caesium is $\Delta t_{pj} \simeq 10^{-26}$ and for Hydrogen $\Delta t_{p2} \simeq 10^{-24}$. As the variance is given by the

second order perturbation term \tilde{h} one can infer that for linear perturbations of about $h \simeq 10^{-20}$ we obtain (leaving rotational invariance untouched $\alpha_{j1} = \alpha$).

$$\alpha_1 = \frac{10^{-40}}{10^{-26}} = 10^{-14} \text{Caesium} \quad \alpha_2 = \frac{10^{-40}}{10^{-24}} = 10^{-16} \text{hydrogen} \quad (8)$$

The Eötvös factor characterising the WEP violation then reads

$$\eta = 2 \frac{|a_1 - a_2|}{|a_1 + a_2|} = \frac{|\alpha_1 - \alpha_2|}{1 + \frac{\alpha_1 - \alpha_2}{2}} \quad (9)$$

Since fluctuations influence only the dynamics of quantum particles, it can best be tested with atomic interferometry. Space missions like GAUGE [25] may provide improved sensitivities. Here we took space–time fluctuations as classical fluctuations of the metric. The effect can be amplified significantly if large coherent systems (e.g. BECs) are taken into account, scaling with the number of particles, or by choosing particle species with small time resolution scales. Generally, our results concerning the amplitude of the effects as a function of resolution scale are also viable for the case where rotational invariance is still valid ($\tilde{\alpha}^{11} = \tilde{\alpha}^{22} = \tilde{\alpha}^{33}$). Thus our model incorporates several effects which are possible outcomes of a theory of quantum gravity.

2.4.2 Quantum vacuum atom wave decoherence

The physics of the vacuum is amongst the most fundamental issues of quantum field theory and GR. The existence of zero point energy is an essential feature of quantum field theory [31]. EM vacuum energy has already seen experimental confirmation through the Casimir effect [32], Lamb shift [33] and spontaneous emission [34]. Recent measurement of the Planckian spectral density of Josephson noise in superconducting circuits [35] confirms the physical reality of EM zero point energy and its ability to interact with the macroscopic world. According to the uncertainty principle, all field components in the SM (and possibly beyond) show a minimum level of fluctuation even at absolute zero temperature, giving rise to zero point energy in vacuum. The role of vacuum energy in cosmology is a subject of intense debate [31, 36, 37]. Does vacuum energy gravitate? The Planckian spectrum for zero point energy is Lorentz invariant but has no UV cutoff, resulting in a formally divergent energy density. The only natural UV cutoff frequency seems to be the Planck frequency but if this value is used the resulting finite vacuum energy density would provide a ‘cosmological constant’ 10^{120} times above the observational limit, measured to be a fraction of the critical density of the Universe. This is the well known cosmological constant problem [31, 38, 39]. A UV cutoff imposed on the Planckian spectrum will lead to Lorentz invariance. Could a signature of this be detectable [29]? The lack of experimental guidance on the gravitational nature of vacuum energy and its role in cosmology has led to many theoretical speculations including quintessence, braneworld and holographic approaches [31, 38]. Quantum field theory in curved spacetime and semiclassical gravity are useful theoretical tools in estimating gravitational effects on quantum fields and their back-reactions [40]. It has important

applications in, e.g. black hole radiation and evaporation [41]. However, semiclassical gravity has been shown to contradict certain experiments [42]. Theoretically, it fails to capture quantum fluctuations of spacetime and would lead to a perfectly homogeneous and isotropic universe even in the presence of fluctuating quantum matter fields [43]. Stochastic gravity [28] is probably a better approximation to quantum gravity but so far has been subject to few experimental tests. The ubiquity of vacuum energy makes all quantum systems into open systems [44]. For example, EM zero point energy may affect electron diffusion in metals [45]. Furthermore, decoherence of free electrons in vacuum by EM zero point energy has been a subject of intense investigations [46, 47]. Due to the weakness of gravitational coupling, the gravitational analogue of the Casimir effect is inconceivable. However, quantum decoherence due to gravitational vacuum fluctuations does not require modifying the boundary conditions of gravity and could be tested using matter wave interferometry under ultra quiet conditions. A number of models exploring quantum and stochastic gravitational decoherence have recently been considered [48–51]. These phenomenological models predict decoherence in terms of the loss of visibility in matter wave interferometry of the form

$$\Delta V \simeq -Am^2t \quad (10)$$

where m is the mass of the quantum particle (which may be an atom like Cs or molecule such as C_{70}), t is the flight time and A is a model dependent form factor. It depends on whether the decoherence effect is due to, e.g. Newtonian gravitational interaction [48, 51] or stochastic gravitational waves [50] or zero-point gravitational fluctuations [51] which also takes into account nonlinear gravitational effects. Furthermore, for cooled and hence indistinguishable quantum particles the form factor A is expected to increase quadratically with the particle number N . In the approach of [51], this factor depends on a UV cutoff frequency w_p/l with a phenomenological parameter λ given by:

$$A \simeq \frac{N^2}{l^3 m_p^2 t_P} \quad (11)$$

where the subscript P denotes a Planck scale quantity, such that t_P is the Planck time. Theoretically, the parameter l may range from order 1 (Planck cutoff scale) to $l \sim m_P/m$ (Compton cutoff scale). Ground based experiments place a lower limit on l as $l > 10^4$. An experimental increase in the limit will provide guidance on effective quantum gravity energy scales, especially in relation to (non)renormalization properties of quantum gravity. In order to test (10) and determine the model dependent form factor A in relation to (11), GAUGE atom interferometry experiments will be carried out by varying the particle measurement parameters including flight time t , particle mass (using two species: Cs and Rb) as well as particle numbers N . Environmental parameters including pressure and temperature will be monitored to determine the possible level of gravitational decoherence effects.

This section has discussed a range of experiments targeting a number of different scientific goals. The main underlying theme has been at the interface

between gravity and quantum mechanics. Any discovery in this regime could lead to fundamental new insights into quantum-gravity or other new forces of nature [52] and would be of profound importance.

3 Proposed payload instrument complement

3.1 Overview of all payload elements

The scientific payload comprises the following payload elements:

- Macroscopic test-masses (LTP) used as source masses for an inverse square law test (IRISL) and as measurement masses for a spin-coupling measurement (IRSC)
- An atom interferometer used for both a microscopic equivalence principle test (QSTEP) and a quantum decoherence study (QDE)
- Three macroscopic test mass pairs housed within a cryogenic science module (CSM) used for a high-precision equivalence principle test (MEPE)
- A polarisable spin-source within the CSM to drive spin-mass coupling forces to be measured by both the LTP test masses and the test mass pairs within the CSM
- An option to supplement the atom interferometry with atom lasers which would enable both short-range inverse square law and spin-coupling tests (SRISL, SRSC)

The payload elements and their layout are identified in Fig. 2.

3.2 The LISA test package

The LISA Test Package (LTP) should be replicated in full. The only change required for GAUGE is to re-orientate the optical bench along the spacecraft axis. In all other respects it should have the same performance parameters as it does for LISA Pathfinder.

3.3 Atom interferometry, QSTEP

The high precision atom interferometer (QSTEP) payload will test the universality of free fall, using the Earth as the source mass with a differential measurement between two species of laser-cooled atoms having different nuclear properties and masses. Rb and Cs are the baseline. Options are ^{87}Rb and ^{85}Rb , in bosonic atomic ensembles, and Rb and ^{40}K or ^{41}K where ^{40}K is a fermion. Atom interferometers in the Mach–Zehnder configuration, (left in Fig. 3) are highly sensitive to inertial forces. In the time domain configuration (right in Fig. 3) proposed for GAUGE each individual atom in the ensemble is coherently split, re-directed and re-combined in a well defined time sequence. The coherent partial wave packet manipulation relies on applying coherent pulses of light which couple the two atomic ground states. This is done with two counter-propagating ‘Raman’ laser beams. An atom absorbs a photon

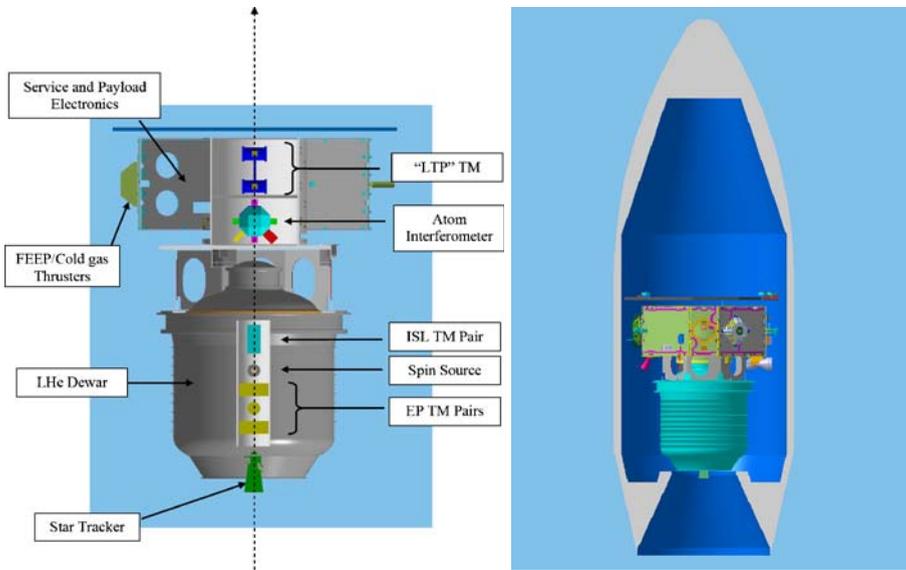


Fig. 2 GAUGE payload element identification and launch configuration

out of one laser beam and is stimulated by the other to re-emit a photon. The recoil momenta of the photons are coherently transferred to the atomic wave, such that it is either equally split, deflected or re-combined. The axis of the photon momentum (laser beam) defines the sensitive direction, and only accelerations in this direction can be sensed. The detection after the third Raman interaction measures the fraction of atoms in each of the two ground states. The ratio between the two ground states gives the phase shift and allows the acceleration to be determined. The two atomic species will be interrogated simultaneously and the difference between them contains the equivalence principle measurement.

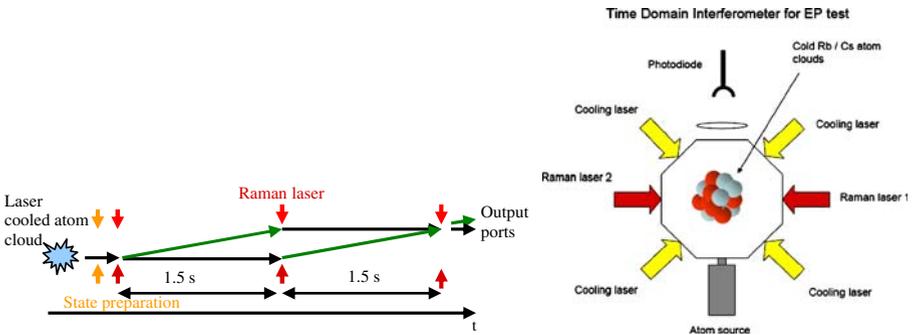


Fig. 3 High precision cold atom interferometry in Mach–Zehnder and time domain configurations

For GAUGE the sensitive axis of QSTEP must be perpendicular to the symmetry axis of the satellite which points in sun direction. Hence, during one orbit the measurement axis will twice align with the Earth direction and twice with the tangent to the orbit path. An equivalence principle violation signal will be modulated once per orbit whereas a modulation due to the gravity gradient will be twice per orbit.

Several payload components are required for the QSTEP:

- In the central vacuum chamber where the atoms are probed the required vacuum level of order 10^{-9} mbar will be maintained by a small ion getter pump and additional getter materials. All lasers are fibre coupled to the beam expander telescopes which are close connected to the chamber. The detection unit contains calibrated photodiodes and a CCD camera for spatially resolved detection. The whole device will be thermally de-coupled from the LPSM. Thermal stability of the physics package is achieved by a combination of passive isolation (multi-layer insulation, conductive de-coupling with titanium mounts), and active temperature control by heaters. Extensive use of CFRP gives superior stiffness and minimises mass and thermal distortions. This vacuum chamber has to be placed in the central tube of the LPSM right below the LTP test mass housing as shown in Fig. 2.
- The lasers and modulation units required to cool, prepare and detect the atoms can be placed in one of the free outer compartments of the LPSM. The light is delivered to the central vacuum chamber using optical fibres.
- Raman laser systems will generate the laser light pulses. Two pre-stabilised lasers will be phase-locked to highly stable microwave frequency reference sources. These units can be placed outside of the inner cylinder with fibre-optic feeds.
- Computer control will autonomously run measurements, calibrations and control phases. In addition, a pre-processing of raw data will be performed. This control unit will be combined with the LPSM on-board computer.

The free fall of the two atom species should be compared with an accuracy of 1 part in 10^{15} . If the interferometer noise is determined by shot noise the sensitivity to accelerations Δa per shot is $\Delta a = N^{-1/2} (k_{\text{eff}} T^2)^{-1}$ where N is the total number of detected atoms, T is the time between the Raman laser pulses and k_{eff} the effective wave vector characterising the momentum transfer. As this is inversely proportional to T long interrogation times are preferred which is one of the reasons for carrying out these experiments in space. However, the residual temperature of laser-cooled atoms is a few μK corresponding to an expansion of the cloud diameter at 3 cm/s which limits T to a few seconds. Taking $T = 1.5$ s gives a total interferometer duration of 3 s. With $N = 10^8$ atoms the sensitivity per interferometer cycle becomes 2.76×10^{-12} m/s² ($k_{\text{eff}} = 22\pi/\lambda_{\text{Rb}}$, $\lambda_{\text{Rb}} = 780$ nm). Assuming well behaved noise this integrates down to $\simeq 2.4 \times 10^{-15}$ m/s² in 1.3×10^6 cycles corresponding to 4×10^6 s or about 50 days.

3.4 Inverse square-law experiments

The proposed GAUGE intermediate range IRISL test is based on the use of the two LTP test masses, in conjunction with the IRISL test mass in the cryogenic module. These three masses are arranged in-line, and each of them can be used as a sensor as well as a source, and also as a drag-free reference sensor. The experimental principle is to measure the ratio between force changes experienced by masses m_1 and m_2 when m_3 is moved, and to verify that this ratio is as expected given the ratio of the separations r_{12} and r_{13} according to the ISL, $\left(\frac{\Delta F_N(r_{13})}{\Delta F_N(r_{23})}\right) = \frac{m_1}{m_2} \left(\frac{r_{23}}{r_{13}}\right)^3$ down to the resolution limit of the experiment.

The ratio will be estimated from $\frac{\Delta F_N(r_{13})}{\Delta F_N(r_{23})} = \frac{x_1 k_1}{x_2 k_2}$ where x_i denotes the observed displacement of mass m_i , and k_i the stiffness of its respective sensor. Assuming that x_i can be measured to sufficient accuracy a meaningful verification of the ISL therefore depends on determining, to sufficiently high accuracy, the ratio between sensor stiffnesses, and the ratio between separations. One other assumption, in what follows, is that the ratio between mass values is known to better than 1ppm. In the precision measurements of the IRISL, the following systematic effects can limit the experimental sensitivity:

- Metrology, in particular the absolute separation between the centres of mass
- Absolute calibration of force sensors (if non-null experiment)
- Density inhomogeneities present in the interacting bodies

For GAUGE, it is proposed to carry out a precision test of the ISL of gravitation at ranges between 10 cm and 1 m, minimising the effect of systematics by exploiting:

- The presence of an external, well-known modulated Earth gravity gradient that can be used for absolute calibration of separation ratios
- The flexibility to use free-floating test masses alternatively as source and test masses, which can be used to calibrate stiffness ratios of force sensors
- A high force sensitivity, masses that are separated by distances much larger than their dimensions can be used, thus minimising density inhomogeneity problems

A ‘proof mass’ acceleration will be measured when the position of “source” masses between 30 cm, and 1 m away are modulated periodically. For simplicity 2 kg masses will be assumed throughout (including that in the cryogenic IRISL). Modulation amplitudes of $d = 4 \times 10^{-3}$ m, compatible with the LTP IS gaps, give acceleration signals between 10^{-12} and 4×10^{-11} ms⁻². An LTP-like electrostatic sensor acceleration noise of 3×10^{-14} ms⁻²/√Hz at 1 mHz will be assumed for all sensors [53]. Then in 10⁶ s we can resolve the induced accelerations to better than 1 ppm at 30 cm and 30 ppm at 1 m. Along the IRISL sensitive (axial) axis, use of the LTP laser interferometry can mitigate noise coupled from the spacecraft, leaving a residual acceleration noise of 7×10^{-15} ms⁻²/√Hz, improving the resolution at 1 m to about 7 ppm. There

is the option of measuring the relative axial spacecraft to TM motion using the laser. The coupling spacecraft-TM can be calibrated by “shaking” the spacecraft deliberately and measuring the TM response. The TM noise can then be corrected for this effect. The gravitational force between two masses separated by r_{13} , including an additional composition-independent Yukawa potential can be parameterised as

$$F_{N+Y}(r_{13}) = G \frac{m_1 m_3}{r_{13}^2} \left(1 + \alpha \left(1 + \frac{r_{13}}{\lambda} \right) \exp(-r_{13}/\lambda) \right) \tag{12}$$

where α characterises the strength of the interaction (relative to gravity) and λ its range. Modulating the distance of mass m_3 by d_3 causes a modulated force on m_1

$$\Delta F_{N+Y}(r_{13}) = -2G \frac{m_1 m_3}{r_{13}^3} \left(1 + \alpha \left(1 + \frac{r_{13}}{\lambda} + \frac{1}{2} \left(\frac{r_{13}}{\lambda} \right)^2 \right) \exp(-r_{13}/\lambda) \right) d_3 \tag{13}$$

A second mass m_2 at a different distance d_{23} from m_3 will see a different force and the ratio between the two will be

$$\left(\frac{\Delta F_{N+Y}(r_{13})}{\Delta F_{N+Y}(r_{23})} \right) = \frac{m_1}{m_2} \left(\frac{r_{23}}{r_{13}} \right)^3 \frac{1 + \alpha \left(1 + \frac{r_{13}}{\lambda} + \frac{1}{2} \left(\frac{r_{13}}{\lambda} \right)^2 \right) \exp(-r_{13}/\lambda)}{1 + \alpha \left(1 + \frac{r_{23}}{\lambda} + \frac{1}{2} \left(\frac{r_{23}}{\lambda} \right)^2 \right) \exp(-r_{23}/\lambda)} \tag{14}$$

and Yukawa terms will escape detection if

$$\left(\frac{\Delta F_{N+Y}(r_{13})}{\Delta F_{N+Y}(r_{23})} \right) - \frac{m_1}{m_2} \left(\frac{r_{23}}{r_{13}} \right)^3 \leq \frac{m_1}{m_2} 3 \left(\frac{r_{23}}{r_{13}} \right)^3 \delta \left(\frac{r_{23}}{r_{13}} \right) \left(\frac{r_{13}}{r_{23}} \right) / \frac{r_{13}}{r_{23}} \tag{15}$$

Assuming $r_{13} = 1.0$ m, $r_{23} = 0.4$ m and $\delta(r_{13}/r_{23}) / (r_{13}/r_{23}) = 2 \times 10^{-6}$ a null result from IRISL would result in limits improving on existing limits for ranges between 10cm and 3m by up to two orders of magnitude. A short-range test of the ISL, SRISL, is also possible in principle using atom interferometry. A mass close to one of the matter wave paths in a spatially dispersed arrangement (Fig. 4) gives an additional phase shift of $\delta\phi = \frac{1}{\hbar} \int \frac{dr}{v} V(r)$, with $V(r) = -\frac{GMm}{r} [1 + \alpha \exp -r/\lambda]$. Assuming 10^8 caesium atoms

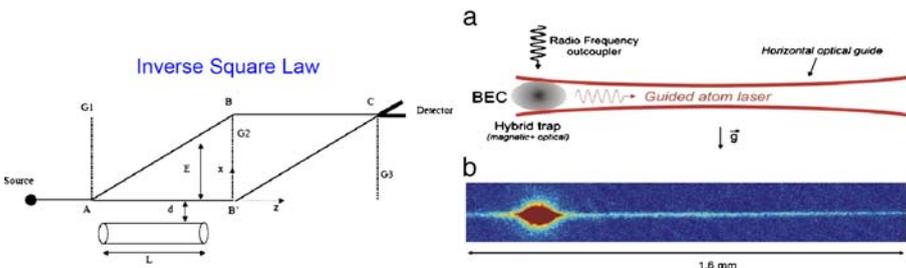


Fig. 4 A short-range ISL test using atom interferometry. *Left* is a general schematic. *Right a* Principle of an atom laser guided in an optical tweezer. *b* Image of the laser after 50ms of propagation in the guide using Rb atoms

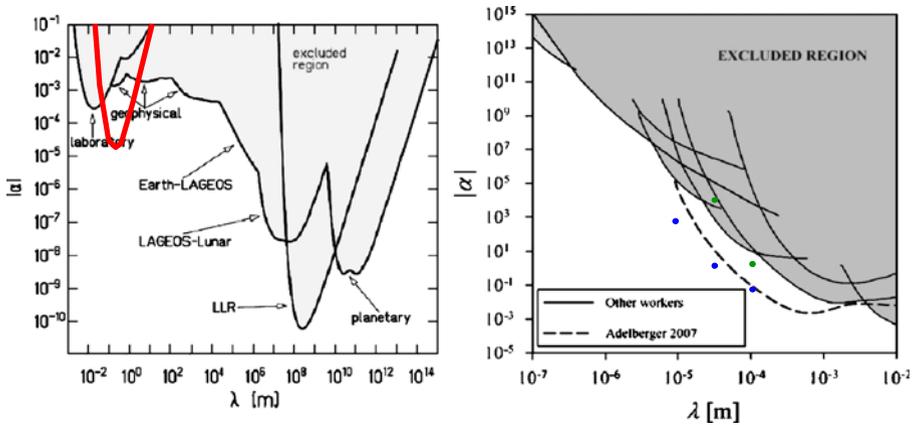


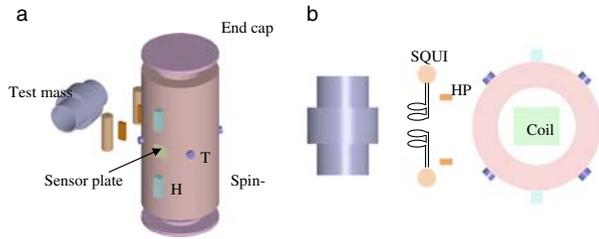
Fig. 5 Sensitivity of GAUGE ISL test to composition-independent Yukawa forces; left is for IRISL, right is for a single-shot SRISL with an over-simplified analysis

traveling at 1 m/s with an effective temperature $\sim 1 \mu\text{K}$, and a 25 cm long gold source mass. The right-hand panel in Fig. 5 shows the sensitivity (blue and green dots using different integration techniques) of an idealised single-shot measurement compared with current ground-based results. In principle the sensitivity should improve as \sqrt{N} where N is the number of repeat shots which could be 10^6 . However a major limitation is beam divergence which is much larger than the 75–375 μm separations assumed in the simplistic calculations so far. This option is worthy of further study but is not yet on firm enough ground to adopt as baseline. One improvement might be to use a guided atom laser source [54]. This was realized starting from the combination of a magnetic trap and a horizontal optical guide, created by a laser Nd:YAG to 1,064 nm with a waist of 20 μm (see Fig. 4). Optical and magnetic potentials create a very confined hybrid trap in which the atoms can be condensed. A low-amplitude radio frequency field transfers a part of the atoms from the trapped state $|F = 1, m_f = -1\rangle$ towards the untrapped state $|F = 1, m_f = 0\rangle$, and a coherent matter wave propagates in the potential formed by the optical guide. A major quality of this device is that the position and direction are controlled by the laser stability and it is possible to achieve better than 1 μm RMS and .1 μrad RMS respectively. The devices can be integrated on minitraps or atomic chip, thus lowering power consumption and volume (mass). Also shown in Fig. 5 (left-hand panel) is the projected sensitivity for the IRISL experiment.

3.5 Spin-coupling experiments

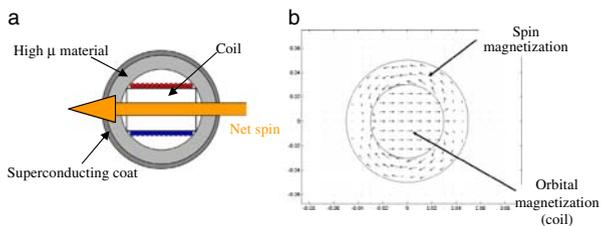
The spin-coupling experiments search for forces between unpolarised nucleons and a spin polarised body (called the spin-source). IRSC proposes to achieve a sensitivity of $g_p g_s = 6 \times 10^{-32}$ at a range of 10 cm improving on previous work by approximately 3 orders of magnitude. A schematic of IRSC is shown in Fig. 6 where unpolarised nucleons constitute one of the superconducting

Fig. 6 **a** Schematic view of the IRSC showing the unpolarised test mass and the spin-source together with the shielded end caps, **b** Top view of the experiment showing the location of the Hall probe (HP)/SQUIDs and heaters (H)/thermometers (T)



test mass pairs in MEPE. The entire IRSC payload is located within the liquid helium dewar and maintained at 1.8 K. A set of magnetic and thermal sensors are incorporated to diagnose potential systematic effects (described below). These comprise SQUIDs, in both magnetometer and gradiometer configurations, together with a Hall probe (HP) to search for modulated and static magnetic fields, and heaters (H) and thermometers (T) to mimic and measure any heating effects. The spin-source, located approximately 12 cm from the test mass, comprises a cylinder of high permeability ferromagnetic material with a high saturation field at low temperature. Figure 7 shows, on the left, a schematic of the spin source with inner/outer dimensions of 3/5 cm and a length of 20 cm. The spin-source generates a macroscopic alignment of spins but at the same time minimises magnetic field leakage to avoid systematic effects through interactions with impurities in the test mass. This is done using a high permeability magnetic shield. A coil on the inside of shield polarises the spins in the shield. This novel design [18] ensures that the field generated by the coil is trapped in the high permeability material. To fully suppress magnetic field leakage the source has high permeability caps which totally enclose the coil. In Fig. 7 a vector field plot of the contributions from the coil and the shield show that outside the spin source the residual magnetic field is negligible. To further suppress any leakage there is a superconducting film of niobium sputter coated onto the outside of the spin-source. This does not affect the spin-coupling signal as superconductivity arises from paired electrons (Cooper pairs) with zero net spin. A convenient feature is that the spins can be modulated electronically, by reversing the current in the coil. The experimental search will look for a spin coupling torque generated at a specific known frequency. To maximise the signal, the spin-source will be operated close to the saturation field of Mu-Metal of approximately 0.7 T. The coil, which polarises the spin-source, must be fabricated from 0.25 mm

Fig. 7 **a** Schematic of the spin source showing the polarising coil, the high permeability cylinder and the superconducting coat. **b** Vector magnetic field plot of the contributions from the coil and the high permeability material



diameter niobium–tin (Nb–Sn) wire with a superconducting transition at 23 K and a critical field of 25 T at 4.2 K. A coil with 4,000 turns and carrying 10 A achieves the required magnetic field. The current has to be periodically stored and quenched to modulate the spin-coupling signal every 1,000 s.

The main problems are systematic effects mimicing spin-coupling interaction. Typically these effects are either magnetic or thermal. Magnetic effects arise from coupling between leakage field/gradient and magnetic impurities in the test mass, and can appear at both the modulation frequency and its first harmonic (f and $2f$). SQUIDs and Hall probes in between the spin-source and the test mass (see Fig. 6) will measure the residual leakage field and place limits on magnetic impurities in the test mass. The Hall probe provides information on the static leakage field due to stable trapped flux in the superconducting films and the residual field in the spacecraft environment. SQUIDs, in magnetometer and gradiometer configurations, provide information on modulated components of the leakage magnetic field due to trapped flux moving in response to the applied field. Systemic magnetic effects are only a problem if there is a net magnetic moment on the test mass due, for example, to ferromagnetic impurities. These can be looked for by modulating the test mass along the sensitive axis (using the test mass suspension) and searching for magnetic fields coupled into the SQUID. Thermal systematics, which can result from hysteretic or eddy current heating in the spin source, are typically $2f$ contributions and appear out of the measurement band, unless the modulation current has a DC offset. Care needs to be taken to limit DC offsets to < 1 mA. Magnetostriction can be a problem if the spin source has non-uniform coefficients of expansion. Energising the spin source with opposite current polarities can shift the centre of mass of the spin source at the modulation frequency, giving a gravitational coupling to the test mass at the signal frequency. This is not expected to be a major systematic uncertainty and it will be possible to measure the spin-source deformation either with an interferometer or capacitive sensor. Figure 6 shows the spin source with plates attached to either side. These plates form a capacitive sensor which can monitor the spin-source and infer whether the expansion due to magnetostriction is uniform for both polarities of current. The required position sensitivity to limit these systematic effects is ~ 0.1 nm. Heaters and thermometers, positioned close to the spin-source, measure and mimic the heating effects for systematic shakedown tests. Each experiment will require approximately 10^4 s. In addition to the systematic tests a spin-coupling measurement will be performed at a period of 1,000s and will run for up to 10^6 s. The systematic tests will be repeated at the end of the run in order to assess the stability of the trapped flux and net polarisation on the test mass. The total experiment time is likely to be 10–15 days. An acceleration sensitivity of $10^{-14} \text{ ms}^{-2}/\sqrt{\text{Hz}}$ at a frequency of 1 mHz, together with an integration time of 10^6 s, would result in the limits shown in the right-hand panel in Fig. 8. At ranges of 10 cm this improves on current constraints from ground based experiments by up to 3 orders of magnitude. A short-range spin-coupling test is also possible in principle using atom interferometry. Placing spin-sources close the matter wave paths

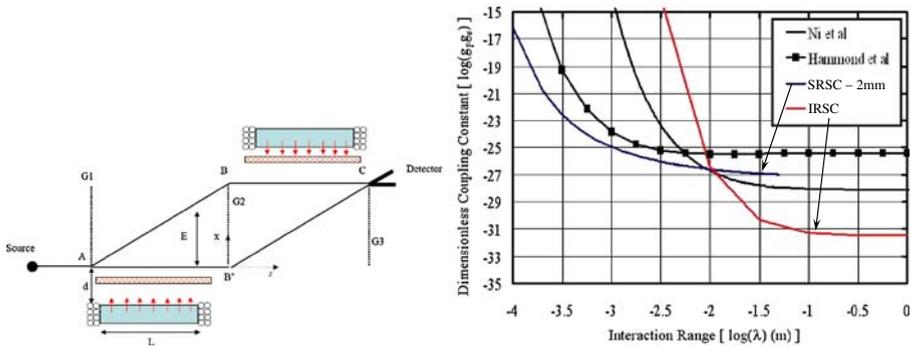


Fig. 8 *Left* a short-range spin-coupling test using atom interferometry. *Right* sensitivity for both IRSC, for an integration time of 10^6 s and SRSC with single-shot atom interferometry using a simplistic analysis

in a spatially dispersed arrangement, as shown in Fig. 8, gives an additional phase shift of $\delta\phi = \frac{1}{\hbar} \int \frac{dr}{v} V(r)$, with $V(r) = g_p g_s \frac{\hbar^2}{8\pi m_{spin}} \sigma \cdot r \left[\frac{1}{\lambda r} + \frac{1}{r^2} \right] \exp(-r/\lambda)$. Assuming 10^8 caesium atoms traveling at 1 m/s with an effective temperature $\sim 1 \mu\text{K}$, and a spin source of dimensions $5 \text{ mm} \times 0.25 \text{ m}$ polarised with 50 A (100 turns). Figure 8 (right) shows the sensitivity (green curve) of an idealised single-shot measurement using atom interferometry compared with current ground-based results. In principle the sensitivity should improve as \sqrt{N} where N is the number of repeat shots which could be as high as 10^6 . However a major limitation with this technique is the beam divergence which is much larger than the $75\text{--}375 \mu\text{m}$ separations assumed in the simplistic calculations so far. This option is worthy further study but is not yet on firm enough ground to adopt as baseline. One potential improvement might be to use a guided atom laser as the source as already noted earlier.

3.6 Macroscopic equivalence principle experiment

The macroscopic test of the equivalence principle will be carried out using a free-fall test in Earth orbit as shown in Fig. 9. Four test mass pairs will be used, each constituting a differential accelerometer. The test mass materials have been chosen to provide sensitivity to the dilaton inspired violations of Damour and Polyakov [1]. Three of the pairs (1–3) provide a closure relationship giving a vital systematic check for any positive violation discovered. The fourth mass pair (4) is orientated such that it should not see any signal. It is otherwise identical to mass pair (1) and so again provides a systematic check. It also acts as a sensitive measurement mass for the intermediate ISL experiment. The masses are all operated at LHe temperature within the cryogenic science module. Readout will be a combination of magnetic (SQUID), optical and capacitive. The measurement uses the Earth as a source mass, but in order to move the signal away from once per orbit, which will be contaminated by

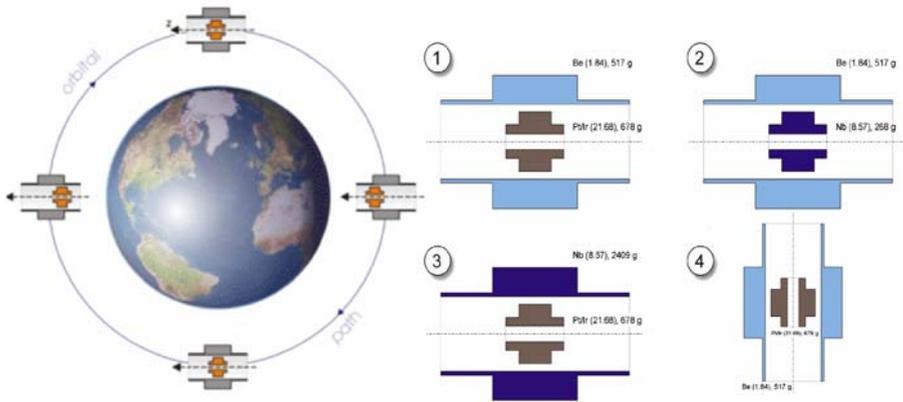


Fig. 9 Orbital free-fall equivalence principle test

other non-ideal effects, the payload will be spun about the probe axis at about three revolutions per orbit.

An orbital free-fall experiment of this type has already been studied in excruciating detail within ESA/NASA by the STEP project [55]. This proposal, although distinct from STEP, retains all the key features relevant to the noise and performance budget. An example noise budget from STEP is shown in Fig. 10. The figures are calculated for a single 20 orbit observation. In the example shown the dominant contributions are from read-out noise and electric potential variations. The science goal of GAUGE is to achieve a sensitivity of 1 part in 10^{18} . We will repeat the experiment at least 20 times with planned experimental set-ups designed to explore systematics and give robustness to the result.

Disturbance	Signal frequency noise (ms^{-2})	Comment
SQUID noise	1.57E-18	Acceleration equivalent of intrinsic noise
SQUID temp. drift	9.58E-19	Regulation of SQUID carriers
Thermal expansion	8.16E-19	Gradient along DAC structure
Differential thermal expansion	5.07E-23	Radial gradient in DAC structure
Nyquist noise	5.23E-19	RMS acceleration equivalent
Gas streaming	1.09E-19	Decaying gas flow, outgassing
Radiometer effect	8.99E-19	Gradient along DAC structure
Thermal radiation on mass	1.86E-22	Radiation pressure, gradient
Var. discharge UV light	3.48E-19	Unstable source, opposite angles on masses
Earth field leakage to SQUID	6.34E-19	Estimate for signal frequency component
Earth field force	4.10E-22	Estimate for signal frequency component
Penetration depth change	3.38E-20	Longitudinal gradient
Electric charge	6.22E-20	Assumptions about rate
Electric potential	1.16E-18	Variations in measurement voltage
Sense voltage offset	2.30E-19	Bias offset
Drag-free residual in diff. mode	3.91E-20	Estimated from SQUID noise
Viscous coupling	1.84E-23	Gas drag + damping
Cosmic-ray momentum	3.33E-21	Mostly directed downwards
Photon radiation momentum	6.03E-19	Unidirectional, downwards
Dynamic CM offset	9.87E-19	Variation about setpoint, converted
Static CM offset limit	1.86E-21	A/D saturation by 2 nd harmonic gg
Trapped flux drift acceleration	7.37E-23	Actual force from internal field stability
Trapped flux changes in SQUID	7.13E-20	Apparent motion from internal field stability
S/C gradient + CM offset	5.79E-33	Gravity gradient coupling to S/C DF residual
Rotation stability	7.19E-20	Centrifugal force variation + offset from axis
Eccentricity subharmonic	8.17E-20	Real part at signal frequency
Helium tide	7.00E-19	Upper limit due to helium motion
Total error	9.21E-18	500m orbit, S/C rotation rate/orbit 2.7, CM period 1466s, differential mode period 1131s, CM offset 1.6E-11 m, gaps 1mm.
RMS error	2.90E-18	

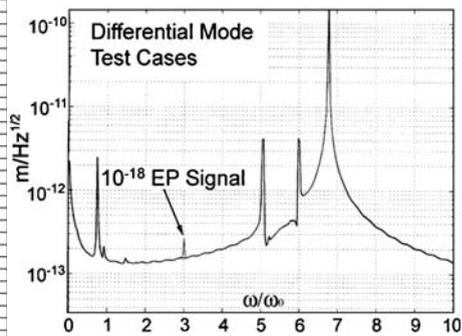


Fig. 10 Error budget and drag-free simulation results for STEP

4 Basic spacecraft key factors

The principle behind the GAUGE spacecraft design has been to identify, as far as possible, existing concepts and technologies that meet the individual instrument requirements. In particular we identify the LISA Pathfinder Science Module (LPSM) including its Inertial Sensor and DFACS. Its functions for GAUGE will be:

- Provision of standard services (Power, Telemetry, etc.) to all payload instruments
- Physical accommodation of all payload instrument control electronics
- Provision of a drag-free environment, either stand-alone using the LTP or in conjunction with sensors within the other experiments
- Physical accommodation of GAUGE Atom Interferometer
- Use of the LTP test masses as part of an inverse square law (ISL) experiment

Attached to the LPSM is the Cryogenic Science Module (CSM), based on existing designs for open-cycle LHe dewars. Its main functions for GAUGE will be:

- Provision of cryogenic environment
- Accommodation of the macroscopic equivalence principle proof-masses
- Accommodation of the spin source for the spin-coupling experiment
- Accommodation of a dedicated test mass pair for the ISL experiment
- Provision of drag-free components, either stand-alone or in conjunction with the LTP, including provision of cold gas for possible thrust control

LISA Pathfinder Science Module Design for GAUGE The science module benefits from the heritage of LISA Pathfinder, due to launch in 2009. LPSM consists of an octagonal structure with a fixed solar array mounted to the upper panel. Volume for the room temperature payload including the LTP and the Atom Interferometer is provided within the central cylinder. In addition the LPSM accommodates all service module equipments required for the mission. Wherever possible LISA Pathfinder systems have been baselined. The electrical system and AOCS equipments are identical to those of LPF. The structure only differs in that the lower interface from the central cylinder is to the CSM rather than a propulsion module.

Cryogenic Science Module for GAUGE Some experiments on GAUGE benefit from operating elements in the CSM in conjunction with elements in LPSM. A key requirement, is that vibrational noise be kept to an absolute minimum. This, together with the need for LEO, precludes the use of active cryo-coolers based on Stirling compressors and mechanical Joule-Thompson systems (too noisy) or cryo-coolers based on sorption coolers and radiative cooling (insufficient performance in LEO). Consequently, the design is based on a passive LHe dewar, sized to ensure sufficient life-time. This has the benefit that He boil-off gas can be used by the drag-free system, as successfully

demonstrated by GP-B. There is a trade-off between capacity and life-time on the one hand, and mass on the other. An additional constraint is set by available launch fairing volume (VEGA). The most relevant dewar heritage comes from GP-B and STEP [56]. GP-B employed a 2500l dewar and had a lifetime of approximately 14 months, whereas the baseline STEP dewar has 230l and is designed for total lifetime (including margin) of approximately 8 months. For GAUGE, different experiments relying on cryogenic conditions will have to be operated in sequence, and as a result the overall life-time needs to be the sum of the anticipated operating time for these experiments. As a first approach, it has been assumed that the outer diameter of a STEP-like dewar can be increased to 1.5 m and still remain shadowed by the solar array at all times. No attempt has been made to assess secondary effects, such as additional residual atmospheric drag or mechanical strengthening or stiffening of the dewar. With a 1.5 m diameter the LHe capacity increases to approximately 500l. Assuming a heat load of 25 mW (as for STEP) this provides a life-time compatible with the science requirements, including margin, of approximately 20 months.

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